



ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ
Δ' ΤΑΞΗΣ ΕΣΠΕΡΙΝΟΥ ΓΕΝΙΚΟΥ ΛΥΚΕΙΟΥ
ΤΕΤΑΡΤΗ 13 ΙΟΥΝΙΟΥ 2018

ΑΠΑΝΤΗΣΕΙΣ ΣΤΗ ΦΥΣΙΚΗ ΠΡΟΣΑΝΑΤΟΛΙΣΜΟΥ

ΘΕΜΑ Α

A1. γ

A2. δ

A3. α

A4. δ

A5. α. Λάθος, β. Σωστό, γ. Λάθος, δ. Σωστό, ε. Λάθος.

B1. α. Σωστή απάντηση : i

β. Αιτιολόγηση :

$$d_2 = \sqrt{(2\lambda_1)^2 + \left(\frac{3\lambda_1}{2}\right)^2} = \sqrt{4\lambda_1^2 + \frac{9\lambda_1^2}{4}} = \sqrt{\frac{25\lambda_1^2}{4}} = \frac{5\lambda_1}{2}$$

$$u = u' \Rightarrow \lambda_1 \cdot f_1 = \lambda_2 \cdot 2f_1 \Rightarrow \lambda_2 = \frac{\lambda_1}{2}$$

$$A' = \left| 2A \cdot \sin \frac{2\pi |d_1 - d_2|}{2\lambda_2} \right| = \left| 2A \cdot \sin \frac{2\pi \left| 2\lambda_1 - \frac{5\lambda_1}{2} \right|}{2 \cdot \frac{\lambda_1}{2}} \right|$$

$$= \left| 2A \cdot \sin \frac{2\pi \frac{\lambda_1}{2}}{\lambda_1} \right| = |2A \cdot \sin \pi| = 2A$$



B2. α. Σωστή απάντηση : iii

β. Αιτιολόγηση :

Αρχή διατήρησης στροφορμής :

$$L_{\text{αρχ}} = L_{\text{τελ}} \Rightarrow m u R = m u' \frac{R}{2} \Rightarrow u' = 2u \Rightarrow \omega' = 4\omega$$

$$\Theta.M.K.E. : W_F = K_T - K_\alpha = \frac{1}{2} I \omega'^2 - \frac{1}{2} I \omega^2 = \frac{3}{2} m R^2 \omega^2$$

B3. α. Σωστή απάντηση : i

β. Αιτιολόγηση :

$$h' = \frac{1}{2} g t^2 \Rightarrow t = \sqrt{\frac{2h}{g}}$$

$$x = u_\Delta \cdot t \Rightarrow 4h = u_\Delta \cdot \sqrt{\frac{2h}{g}} \Rightarrow 16h^{\frac{3}{2}} = u_\Delta^2 \cdot \frac{2h}{g} \Rightarrow u_\Delta^2 = 8gh$$

Εξίσωση συνέχειας

$$\Pi_r = \Pi_\Delta \Rightarrow A_r \cdot u_r = A_\Delta \cdot u_\Delta \Rightarrow 2A_\Delta \cdot u_r = A_\Delta \cdot u_\Delta \Rightarrow$$

$$u_\Delta = 2u_r \Rightarrow u_\Delta^2 = 4u_r^2 \Rightarrow 8gh = 4u_r^2 \Rightarrow u_r^2 = 2gh$$

$$\text{Bernoulli} : P_r + \frac{1}{2} \rho u_r^2 = P_\Delta + \frac{1}{2} \rho u_\Delta^2 + \rho gh \Rightarrow$$

$$P_r - P_\Delta = \frac{1}{2} \rho \cdot 8gh + \rho gh - \frac{1}{2} \rho \cdot 2gh \Rightarrow$$

$$P_r - P_\Delta = 4\rho gh \Rightarrow P_r - P_\Delta = 2\rho u_r^2$$



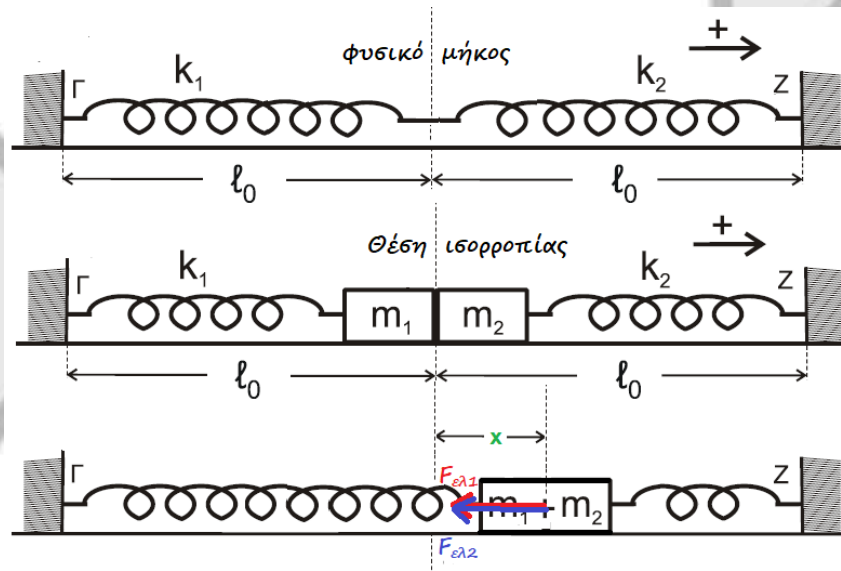
ΘΕΜΑ Γ

$$\Gamma 1. u_1 = u_{\max(1)} \Rightarrow \omega_1 \cdot A = \sqrt{\frac{k}{m_1}} \cdot A \Rightarrow u_1 = 2 \text{ m/s}$$

$$\text{ΑΔΕΤ : } A = \Delta \ell$$

$$\sum F = -F_{\varepsilon\lambda_1} - F_{\varepsilon\lambda_2} = -kx - kx = -2kx = -Dx \Rightarrow D = 2k \text{ (Α.Α.Τ.)}$$

$$u_{\max} = u_K \Rightarrow \omega_z \cdot A_z = 1 \Leftrightarrow \sqrt{\frac{2k}{2m}} \cdot A_z = 1 \Rightarrow A_z = 0,2\text{m}$$



$$\Gamma 2. x = A \cdot \eta \mu \omega t \Rightarrow x = 0,2 \cdot \eta \mu 5t \text{ (SI)}$$

$$\omega = \sqrt{\frac{2k}{2m}} = 5 \text{ r/s}$$

$$\Gamma 3. \Delta t = \frac{T}{4} = \frac{2\pi \sqrt{\frac{2m}{2k}}}{4} = 0,1\pi \text{ s}$$



ΘΕΜΑ Δ

$$\Delta 1. \Sigma_1 : \sum F = 0 \Rightarrow$$

$$T_1 = m_1 g \Rightarrow$$

$$T_1 = 30 \text{ N}$$

$$\text{ΤΡΟΧΑΛΙΑ : } \sum T = 0 \Rightarrow$$

$$T_1 \cdot r_2 = T_2 \cdot r_1 \Rightarrow$$

$$30 \cdot 0,2 = T_2 \cdot 0,1 \Rightarrow$$

$$T_2 = 60 \text{ N}$$

$$\Delta 2. \sum F = m_2 \cdot a_{\text{cm}} \Rightarrow$$

$$W_{x_2} - T_{\text{στ}} = m_2 \cdot a_{\text{cm}} \Rightarrow$$

$$T_{\text{στ}} = 120 - 20 \cdot a_{\text{cm}} \quad (1)$$

$$\sum T = I \cdot \alpha_{\gamma\omega\nu} \Rightarrow$$

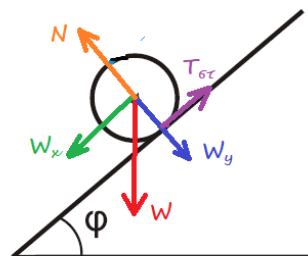
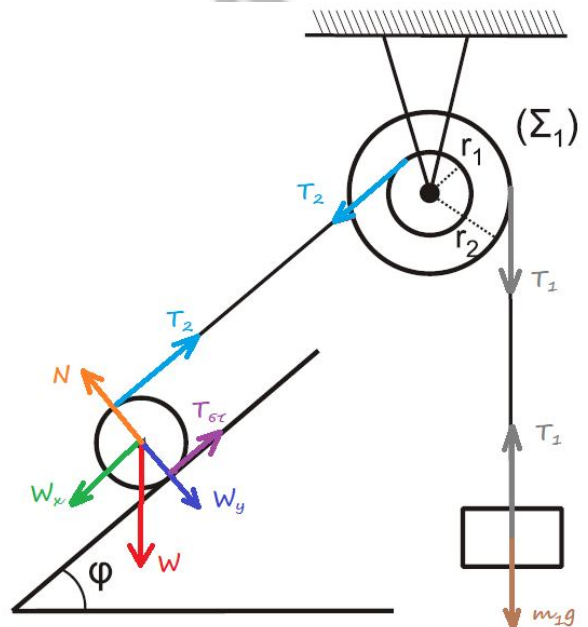
$$T_{\text{στ}} \cdot R = \frac{1}{2} m_2 \cdot R^2 \alpha_{\gamma\omega\nu} \Rightarrow$$

$$T_{\text{στ}} = 10 \cdot a_{\text{cm}} \quad (2)$$

$$(1), (2) \Rightarrow 10 a_{\text{cm}} = 120 - 20 a_{\text{cm}} \Leftrightarrow$$

$$30 a_{\text{cm}} = 120 \Leftrightarrow$$

$$a_{\text{cm}} = 4 \text{ m/s}^2$$



**Δ3. ΤΡΟΧΑΛΙΑ**

$$\sum \tau = I \cdot \alpha_{\gamma\omega\nu} \Rightarrow T_1 \cdot r_1 = 0,48 \cdot \alpha_{\gamma\omega\nu} \Rightarrow$$

$$T_1 = \frac{0,48}{0,2} \cdot \frac{\alpha}{R_2} \Rightarrow T_1 = 12\alpha \quad (1)$$

ΣΩΜΑ

$$\sum F = m_1 \cdot \alpha \Rightarrow m_1 g - T_1 = m_1 \alpha \Rightarrow$$

$$T_1 = m_1 g - m_1 \alpha \Rightarrow T_1 = 30 - 3\alpha \quad (2)$$

$$(1), (2) \Rightarrow 12\alpha = 30 - 3\alpha \Leftrightarrow 15\alpha = 30 \Leftrightarrow \alpha = 2 \text{ m/s}^2$$

$$\Delta 4. x = \frac{1}{2} \alpha \cdot t^2 \Rightarrow 0,25 = \frac{1}{2} \cdot 2 \cdot t^2 \Rightarrow t^2 = 0,25 \Rightarrow t = 0,5 \text{ s}$$

$$\alpha = \alpha_{\gamma\omega\nu} \cdot R_2 \Rightarrow \alpha_{\gamma\omega\nu} = \frac{\alpha}{R_2} = \frac{2}{0,2} = 10 \text{ r/s}^2$$

$$K = \frac{1}{2} I \cdot \omega^2 = \frac{1}{2} \cdot 0,48 \cdot (10 \cdot 0,5)^2 = \frac{1}{2} \cdot 0,48 \cdot 25 = 6 \text{ J}$$